SCALE-SPACE METHOD OF IMAGE RINGING ESTIMATION

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ABSTRACT

Suppression of ringing effect is a challenging problem. It is mainly caused by absence of effective methods of ringing artifact detection. In this paper we introduce a ringing estimation method based on scale-space analysis. The estimation shows good results for low-pass filtered test images and in adaptive image deringing.

Index Terms— Ringing estimation, total variation, scale space, adaptive deringing

1. INTRODUCTION

Development of image enhancement methods is one of the most important image processing tasks. Ringing effect (Gibbs phenomenon) appears in images as oscillations near sharp edges. It is a result of a cut-off of high-frequency information. Ringing can appear as a result of image compression, image upsampling and other applications. An example of this effect can be seen in old video stored in analog format (Fig.1).

One of the main problems of image deringing is to detect the presence of ringing effect and to estimate the necessary ringing suppression level. But there is no algorithm which estimates ringing level in the general case.

There are image ringing estimation algorithms to measure ringing effect for a specific problem. In [1] wavelet decomposition is used and ringing effect is measured for JPEG-2000 compression as a difference between correlations of neighbor coefficients of different wavelet subbands. The problem of image deringing after JPEG-2000 compression is also considered in [2], [3].

Some metrics were developed to control image deringing as a postprocessing. Regularization parameter estimation for image deringing using MAP approach is proposed in [4]. For the problem of image deringing after resampling, regularization parameter is estimated using information on the initial low resolution image [5]. In [6], the ringing metrics is defined as maximum of the differences between pixel values of the reference image and the processed image in the edge neighborhood. The size of this neighborhood is fixed a priori.



Fig. 1. A video frame with a strong ringing effect.

In [7], the presence of ringing effect is detected by comparing the directions of image gradients at different scales.

The work [8] does not introduce a ringing estimation method, but it presents an algorithm to find regions where the ringing effect is the most visible. It is based on luminance masking and texture masking as typical for the human visual system.

In this article, we suggest new general ringing estimation algorithm based on total variation (TV) control. The TV was first used in image enhancement by Rudin, Osher and Fatemi [9] for image denoising. General relations between TV and ringing effect can be found in [10].

2. ONE-DIMENSIONAL TOTAL VARIATION

In one-dimensional case, Total Variation functional is defined as

$$TV(f) = \int_{a}^{b} |f'(x)| dx.$$

In a discrete case $a = x_0 \le x_1 \le \ldots \le x_n = b$, it looks as:

$$TV(f) = \sum_{i=1}^{n} |f(x_i) - f(x_{i-1})|.$$

We also consider weighted TV (WTV) with weight function w(x):

$$TV(f,w) = \int_{a}^{b} |f'(x)|w(x)dx.$$

In the discrete case it looks as

$$TV(f,w) = \sum_{i=1}^{n} |f(x_i) - f(x_{i-1})| w\left(\frac{x_{i-1} + x_i}{2}\right).$$

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3. RINGING ESTIMATION FOR ONE-DIMENSIONAL EDGE

We consider the problem of ringing level estimation for step edge with width *d*:

$$\overline{f}_d(x) = \begin{cases} 0, & x < -d/2, \\ x/d + 1/2, & -d/2 \le x < d/2 \\ 1, & x \ge d/2. \end{cases}$$

at the interval with the length $\gg d$. In the discrete case, $TV(\overline{f}_d) = 1$ for any grid.

Ringing effect can be generated by ideal low-pass filter which truncates high frequency data. We implement it using sinc interpolation of the step edge $\overline{f}_0(x)$ given at the discrete set $\{x_k\}, x_k = dk + \frac{d}{2}$ with sampling period d:

$$f_d(x) = \sum_k \overline{f}(x_k) \operatorname{sinc} \frac{x - x_k}{d}, \qquad (1)$$

where $\operatorname{sinc}(x) = \frac{\sin \pi x}{\pi x}$. We call here the value *d* as ringing half-period. It is an analog of step edge width for edges with ringing effect.

Real edges are corrupted by noise, so this fact is to be considered too. In this work, we analyze the case of additive uniform noise $f_{d,n}(x) = f_d(x) + \xi_n(x)$, $\overline{f}_{d,n}(x) = \overline{f}_d(x) + \xi_n(x)$, where $\xi_n(x)$ is uniformly distributed random function which values are in (-n/2, n/2) range. We consider $n \le n_0$, where n_0 is the maximum noise value.

3.1. Edge width estimation

For further scale-space TV analysis, we need to make a definition of the edge width.

To find edge width for an arbitrary edge f(x), we approximate it by the edge $\overline{f}_d(x)$ (3). We seek for minimum f_0 and maximum values f_1 of f(x) in a neighborhood of the edge center. For simplicity, we consider $f_0 = 0$, $f_1 = 1$. The size of this neighborhood is chosen a priori and represents the maximum considered edge width.

Next we find the coordinates of intersections of y = f(x)with $y_0 = 1/4$ and with $y_1 = 3/4$, draw a line through these points and find x_0 and x_1 as it is shown in Fig.2. In the case of multiple intersections we take the average of intersection points. We call the obtained value as the edge width.

To reduce the influence of ringing artifact and noise to the edge width, we smooth the edge using Gauss filter with radius $\frac{3}{4}d$, calculate the values f_0 and f_1 for the smoothed edge and recalculate edge width using these values.

3.2. Scale-space TV analysis

We performed an experimental analysis of edge TV with different widths d at different scales σ . Real edges are not infinite. To take into account only several first ringing oscillations, we use weighted TV with Gaussian weight $w_{\alpha d}(x) =$



Fig. 2. Edge width estimation illustration. For the shown case, the estimated edge width is 4.3 pixels.

 $e^{-\frac{x^2}{2(\alpha d)^2}}$, where α controls the number of considered ringing oscillations. To find the differences between edges with ringing effect and edges without it, we analyze the functional

$$TV(f,\sigma,w_{\alpha d}) = TV(f * G_{\sigma}, w_{\alpha d}),$$
(2)

where $f * G_{\sigma}$ is a convolution of f with Gauss filter with radius σ .

To design an algorithm to find the value σ_1 that best discriminates between edges with ringing artifact and edges without ringing artifact for fixed d, fixed maximum noise level n_0 and given parameter α , the following analysis has been performed:

A set of 5000 step edges without ringing effect $\overline{f}_{d,n}$ (set A) and 5000 edges with ringing effect $f_{d,n}$ (set B) with random noise levels $0 \le n \le n_0$ for each edge was generated. For every σ , the intervals of values of (2) were calculated for both sets A and B. If these intervals do not intersect, σ can be used for ringing detection. The intervals of values of function (2) for d = 10, $n_0 = 0.1$ and $\alpha = 3$ are shown in Fig.3. It can be seen that there is a set of σ (marked as yellow area) which can be used to distinguish between sets A and B.

TV values of edges with ringing artifacts are greater than TV values of edges without ringing effect. We calculated minimal value of TV of edges with ringing artifact

$$g^*(d,\sigma) = \min TV(f_{d,n},\sigma,w_{\alpha d})$$

and maximal value of TV of edges without ringing artifact

$$g_*(d,\sigma) = \min TV(\overline{f}_{d,n},\sigma,w_{\alpha d}).$$

Next we found σ that corresponds to the maximal gap between $g^*(d, \sigma)$ and $g_*(d, \sigma)$:

$$\sigma_1(d) = \arg\max\left(g^*(d,\sigma) - g_*(d,\sigma)\right). \tag{3}$$

The calculated values of $\sigma_1(d)$ for $n_0 = 0.1$ and $\alpha = 3$ for different d are shown in Fig.4.

The function $\sigma_1(d)$ is close to linear function, its random fluctuations are caused by noise and we use the approximation

$$\sigma_1(d) = m(\alpha, n_0)d.$$



Fig. 3. Scale-space TV analysis for noisy edges with width d = 10, maximum noise level $n_0 = 0.1$ and $\alpha = 3$ (number of oscillations ~ 3). Blue area is the range of values of function (2) for edges with ringing effect $\overline{f}_{d,n}$. Red areas is the range of values of (2) for edges without ringing effect $f_{d,n}$. Black area is the intersection between blue and red areas. Yellow area corresponds to possible σ which can be used to separate red and blue areas.



Fig. 4. The results of σ_1 calculation (3) for $n_0 = 0.1$ and $\alpha = 3$ for different *d*. Thin line is a linear approximation of function $\sigma_1(d)$.

For $\alpha = 3$ and $n_0 = 0.1$, we use $m(\alpha, n_0) = 0.19$. For $\alpha = 3, n_0 = 0.2, m(\alpha, n_0) = 0.25$. Experiments have shown that $m(\alpha, n_0)$ does not depend too much on α for reasonable α values ($\alpha > 2$).

This enables us to consider the value

$$R_E^*(f,d) = TV(f,m(\alpha,n_0)d,w_{\alpha d})$$

as edge ringing level. For the case of edges with an arbitrary height, we perform a normalization. For $\sigma = d$, the values $g_*(\sigma)$ and $g_d^*(\sigma)$ were found close, so it is natural to divide the value R_E^* by $TV(f, d, w_{\alpha d})$. Ringing value takes the form:

$$R_E(f,d) = \frac{TV(f,m(\alpha,n_0)d,w_{\alpha d})}{TV(f,d,w_{\alpha d})}.$$

To make a decision about the presence of ringing effect for edge f with edge width d, we compare the calculated ringing

level $R_E(f, d)$ with precalculated threshold functions

$$G_*(d) = g_*(d, m(\alpha, n_0)d),$$

 $G^*(d) = g^*(d, m(\alpha, n_0)d).$

If $R_E(f,d) \leq G_*(d)$, we assume that the edge does not have ringing artifact. If $R_E(f,d) \geq G^*(d)$, we assume that the edge has ringing artifact. In practice, signals are not perfectly bandlimited and ringing effect is weakened. Thus $R_E(f,d)$ can fall into $(G_*(d), G^*(d))$ interval. The decision in this case needs additional analysis for each specific image class. For example, for linearly interpolated images or for video stored in analog format, we assume that ringing effect is presented in this case.

The calculated threshold functions $G_*(d)$ and $G^*(d)$ for $n_0 = 0.1$ and $\alpha = 3$ for different d are shown in Fig.5.



Fig. 5. Thresholds $G_*(d)$ and $G^*(d)$ for $n_0 = 0.1$ and $\alpha = 3$.

4. RINGING ESTIMATION FOR TWO-DIMENSIONAL IMAGES

We consider the problem of ringing estimation for twodimensional images with uniform ringing effect. It means that cut-off frequency is constant and ringing half-period Dis the same for any edge normal cross-section. We apply the following algorithm:

1. Perform edge detection and extract edge normal crosssections $f_k, k = 1, 2, ..., N$ for strong isolated edges [11].

2. Estimate edge widths $d_k = d(f_k)$ for all k and calculate ringing half-period D. For real images, edge width is different for different edges due to blur and noise. We treat d_k as a distribution and estimate D as the value of the highest density of this distribution. To reject noise and blur outliers, we take only edges where $|d_k/D - 1| \le 0.2$.

3. For every edge we calculate its ringing level $R_E(f_k, D)$, and we define image ringing level R_I as an average of all obtained edge ringing levels.

4. At the last stage, we compare R_I with the precalculated ringing thresholds $G_*(D)$ and $G^*(D)$ and make the decision about the presence of ringing artifact in the image.

5. RESULTS

The effectiveness of the proposed ringing estimation algorithm was shown by image deringing applications.

1. Correspondence between the proposed ringing level and existing image deringing algorithm. Ringing level was calculated for the initial low-resolution image, for the image resampled by regularization method [11] and for the resampled image postprocessed by deringing method [5]. The results are given in Fig.6.

It shows that the proposed ringing estimation algorithm can be used to control ringing level in image deringing applications.



Fig. 6. Ringing estimation for image deringing after resampling [5]. Left image: source image upsampled by pixel replication, $R_I = 1.05$. Middle image: image interpolated by regularization-based method with low regularization [12], $R_I = 2.20$. Right image: interpolated image postprocessed by deringing after resampling [5], $R_I = 1.06$.

2. Automatic image deringing for real video. The strength of the deringing algorithm [5] was consecutive increased until ringing level R_I of the processed video frame was less than the threshold G^* . A result is shown in Fig.7



Fig. 7. Automatic image deringing. Left image: original image with ringing effect, $R_I = 1.44$. Right image: the result of automatic deringing with ringing level control, $R_I = 1.20$.

6. CONCLUSION

Scale-space ringing level estimation for one-dimensional functions and two-dimensional images was proposed. Very promising results were achieved for deringing after resampling and adaptive deringing using ringing level control in the presence of noise.

Future work on the proposed ringing level estimation method includes additional refinement of the ringing criterion for different image classes and edge width estimation.

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